"Common core" standards, student test scores in math computation, and the implications for chemistry instruction

> Presented 7/28/2012 to the Math in Chemistry symposium at BCCE By Rick Nelson, Retired Instructor EANelson@ChemReview.Net

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Good afternoon.

Let me start with an apology. I am going to go a bit too fast. But I will put up a web address at the end where you may view the any slides of interest at your leisure.

I am going to restrict my talk today to the question of: "How can we help students solve the type of calculations

That we assign them in general chemistry?"

Vote for ONE:

To start *Gen* Chem, it is *most* important that students have background in

- A. Use of a Calculator
- B. The Theory of Math
- C. Math Computation

I'd like to ask you to read and be ready to vote on this.

$$\begin{split} \mathscr{E} &= \mathscr{E}_{\text{cell}}^{\circ} - \frac{0.0591}{n} \log(Q) \\ &= 1.76 - \frac{0.0591}{2} \log \left(\frac{[\text{Zn}^{2+}][\text{VO}^{2+}]^2}{[\text{VO}_2^{+}]^2[\text{H}^{+}]^4} \right) \\ &= 1.76 - \frac{0.0591}{2} \log \left(\frac{(1.0 \times 10^{-1})(1.0 \times 10^{-2})^2}{(2.0)^2(0.50)^4} \right) \\ &= 1.76 - \frac{0.0591}{2} \log \left(4 \times 10^{-5} \right) = 1.76 + 0.13 = 1.89 \, \text{V} \\ &- \text{Zumdahl, 5th edition} \end{split}$$

In Gen Chem, we ask students to solve problems like this

Slide 4

$$u_{\rm rms} = \sqrt{\frac{3\left(8.3145\,\frac{\rm J}{\rm \textrm{\emph{K}}\cdot\rm{pard}}\right)\!(298\,\textrm{\emph{K}})}{4.00\times10^{-3}\,\frac{\rm kg}{\rm pard}}}} = \sqrt{1.86\times10^6\,\frac{\rm J}{\rm kg}}$$
 Since the units of J are kg·m²/s², this expression becomes
$$\sqrt{1.86\times10^6\,\frac{\rm kg\cdot m^2}{\rm kg\cdot s^2}} = 1.36\times10^3\,\rm m/s$$
 -- Zumdahl, 5th Ed. p. 218

And this...

Vote for ONE:

To start *Gen* Chem, it is *most* important that students have background in

- A. Use of a Calculator
- B. The Theory of Math
- C. Math Computation

In chem, which ONE is MOST important?

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All of these are important but in			
chemistry, if you had to pick ONE, which	ch is most important?		
How many vote for A:	B:	C:	
(The vote was about 05% for math cor	nnutation)		

(The vote was about 95% for math computation).

For ~10⁺ year faculty:

(Vote for ONE:)

Since 2002, I have seen the *computation skills* of first-year students:

- A. Improve substantially
- B. Improve
- C. Not change
- D. Decline
- E. Decline substantially

	•	•	•	ve taught for more fossilized joints to	•
for A :	_ B:	C:	D :	E:	
The average OK. Thank		`	E received by	far the most votes.)

The "Monty Python Group" Experiments

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For the past 5 years, I've been working on experiments with a small team of instructors, and our goal is to improve student achievement and retention in first-year Chem, and because that's the Holy Grail, we call ourselves.....

Dahm: Rowan Engineering Chem (2 sem. Gen Chem in 1 sem.)

2006

ACS Exam:

(not given)

Lab Periods:

10 for Lab

5 for Lecture

This started at Rowan University in NJ. My buddy Don Dahm was teaching engineering chemistry, which at Rowan is two semesters of Gen Chem on a one semester schedule, and Don was having to lecture during 5 of his 15 lab periods to cram all the content in. So Don was not happy.

Dahm's "Calcs In Chem" Expt.

1. Homework: Review Math for Topic

Learn Chem Facts

Practice Problem Solving

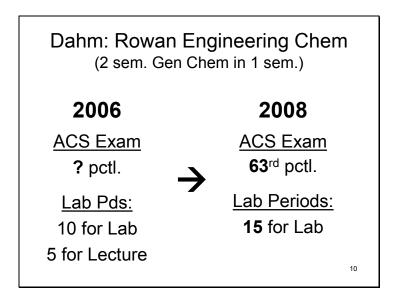
2. Lecture: Active learning of *concepts*

3. Quizzes: Weekly

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So we decided to try an experiment: to write tutorials that moved a *part* of the lecture into homework, so there would be more time during lab and lecture for *active learning*.

We included a review of the math needed for each topic and a weekly quiz to "encourage" students to keep up with the homework.



And after two years of trial and lots of errors, scores on the ACS Gen Chem Final Exam for Don's students were at the 63th percentile. (which we thought was not bad for Gen Chem in one semester).

Best of all, Don was able to go from 10 labs to the full 15.

(By 2011, the ACS percentile was 64, and Don had about 20% fewer drops.)

And Don is happy. He's doing more chemistry.

Use of "Calculations in Chemistry" In Prep Chem at Frostburg:

- 70% of Prep Chem enrolled in Gen Chem
- 75% of those passed first semester.

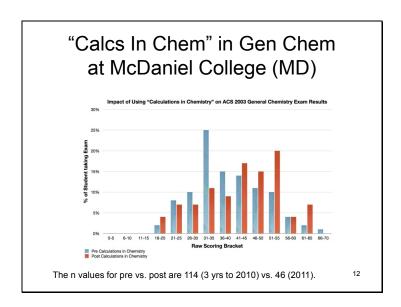
"My belief is that we rescued many of these students from failing General Chemistry."

> -- Dr. Mary Mumper Paper #4 -- 11/2009 <u>Newsletter</u> CCCE/<u>DivCHED</u>/ACS

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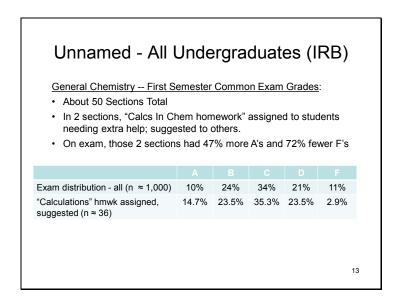
At Frostburg State in Maryland, Dr. Mary Mumper adopted a portion of Don's homework tutorials as the textbook for a new course Prep Chem.

Over the first 3 experiment semesters, 70% from Prep Chem enrolled in General Chemistry, and 75% Of those passed first semester. This is what Dr. Mumper wrote in her report to faculty.



In 2010 at McDaniel College, Dr. Peter Craig used Don's tutorials for homework assignments in General Chemistry. Each year, Dr. Craig uses ACS exam as his final.

The x-axis has the ACS score ranges. The blue bars are the distribution of the scores for the 3 years *before* Dr. Craig used the lessons. The red bars are the scores for the year that he used the lessons. Blue before, red after. The rise in median score is from about the 45th to about the 60th percentile.



Finally, last year at a school where there was a concern about the IRB paperwork: 1000 students in Gen Chem took the first semester common exam, and in the small sample that had used Don's online homework lessons, there were 47% more A's and 72% fewer F's.

Those are the Monty Python results so far.

As part of our lessons, we *teach* quite a bit of math. Let me explain why we think we need to teach math in chemistry.

Virginia Math Results:

- Stanford 9 standardized test given statewide
- 1995: normed at 50th percentile

VA all students			Grade 9		
	1998	1999	2000	2001	2002
Total Math	54	55	55	55	55

4

I got involved in the "math and chemistry" issue about 8 years ago, when I was working for my faculty organization on a task force looking at why so many Virginia students entering college needed remediation in math.

When we looked at the test scores for students, in "Total Math," Virginia scores were above national average – the 50th percentile -- and steady. But to me, those scores didn't look right. So I looked in the back of the report,

Two subtests were reported described as

- "Math Problem Solving, which focuses on reasoning skills, and
- Math Procedures, which measures the student's facility with computation."

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and I found that on the test VA was using, "Total Math" was actually a composite of two **sub**tests: one on math *reasoning* and the other on math *computation*

All students			Grade 9		
	1998	1999	2000	2001	2002
Total Math	54	55	55	55	55
Problem Solving (Reasoning)	58	61	63	64	65
Procedures (Computation)	46	44	42	41	39

Here's that data -- from 80,000 students/year in 130 independent districts. In math **reasoning**, scores were way above the 50th percentile and getting higher every year.

But in **computation**, the math that's important in chemistry, scores were low and getting lower every year.

All students	Grade 9				
	1998	1999	2000	2001	2002
Total Math	54	55	55	55	55
Problem Solving (Reasoning)	58	61	63	64	65
Procedures (Computation)	46	44	42	41	39

This raised two questions. One: When your state average in computation is at the 39th percentile, what percentage of these students are going to be ready for the rigor and pace of college chemistry?

Two: Getting a lot better at reasoning in math, but getting a lot worse at solving calculations – no transfer -- Is that what you'd expect?

When the math issue came up several months later at a chemistry meeting in New Jersey, Don and I went looking for data in other states.

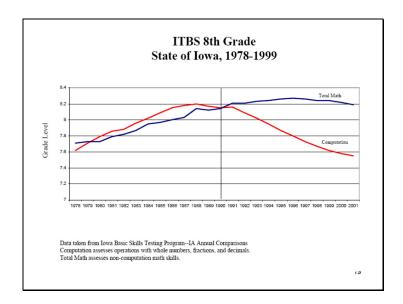
Next three graphs from:

Dr. Tom Loveless, Director Brown Center on Education Policy at the Brookings Institution Presentation on Math Reform at AEI, March 4, 2002

http://www.aei.org/files/2002/03/04/20030326_loveless.pdf

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This report was found online from Tom Loveless at the Brookings Institution. Dr. Loveless said the best data was for the state of



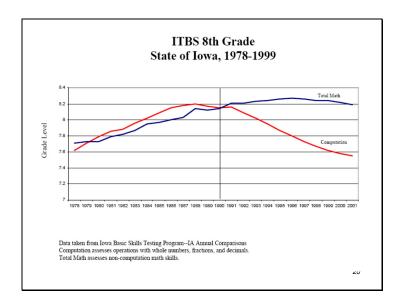
lowa. In Iowa, like Virginia, each K-12 district does its own textbook adoption So you get a random sample of curricula nationally, but lowa gave the same test for over 20 years.

This graph starts in 1978 and goes to 2001.

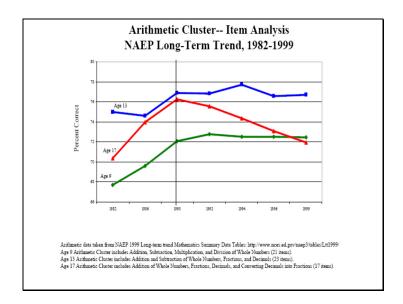
Do you see a problem? What is it? When does the problem start?

Out here at the right: does total math hide the computation problem? Just like in Virginia?

Note from 98 to 01 – these results are convergent with Virginia: Total math flat; computation low and going lower.



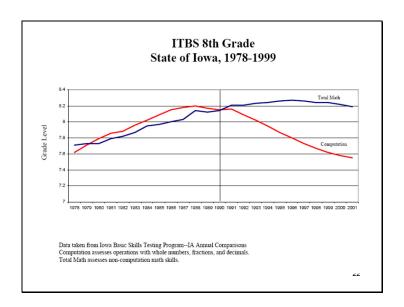
Note also that something is missing. Total math is a composite. What Dr. Loveless did not graph (his focus was computation) are the "concepts" and "reasoning" subtests on the ITBS. In lowa, reasoning and concepts went up, but that did not help with the math needed for chemistry.



Dr. Loveless also looked at a **nation-wide** measure: The National Assessment of Educational Progress (NAEP -- the "nape") the "nation's report card," given every two years in every state.

In the **arithmetic** that we do quite a bit of in chemistry, the RED line is for the 17 year olds that we are most concerned with.

For the 17-year-olds in red, when is it GOOD? When is it BAD?



Like computation in Iowa?

$$\mathcal{M} = \frac{\frac{dRT}{P}}{P}$$
=\frac{(3.09 \text{ g/L})(0.0821 \text{ L-atm/mol-K})(304 \text{ K})}{(735/760) \text{ atm}}
= 79.7 \text{ g/mol}

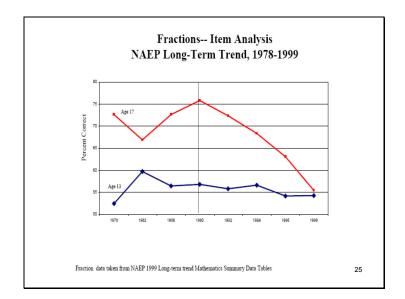
-- Brown, Lemay, 8th Ed. p. 368

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In chemistry, we need students to solve some complex fractions. Here we have a fraction times a fraction over a fraction.

$$u_{\rm rms} = \sqrt{\frac{3\left(8.3145\,\frac{\rm J}{\it K\cdot paol}\right)(298\,\it K)}{4.00\times 10^{-3}\,\frac{\rm kg}{\rm paol}}} = \sqrt{1.86\times 10^6\,\frac{\rm J}{\rm kg}}$$
 Since the units of J are kg·m²/s², this expression becomes
$$\sqrt{1.86\times 10^6\,\frac{\rm kg\cdot m^2}{\rm kg\cdot s^2}} = 1.36\times 10^3\,\rm m/s$$
 -- Zumdahl, 5th Ed. p. 218

And the top fraction here involves 3 fractions.



Dr. Loveless looked at fractions on the NAEP and found, for the 17 year olds, fluctuation before 1990, then a dramatic decline From **24**% wrong in 1990 to **44**% wrong in 1999, nationwide.

When their fundamental background in fractions is down here, What's happens when these students get to

$$u_{\rm rms} = \sqrt{\frac{3\left(8.3145 \frac{\rm J}{\rm \c{K \cdot pool}}\right)(298 \c{K}\right)}{4.00 \times 10^{-3} \frac{\rm kg}{\rm \c}}} = \sqrt{1.86 \times 10^6 \frac{\rm J}{\rm kg}}$$

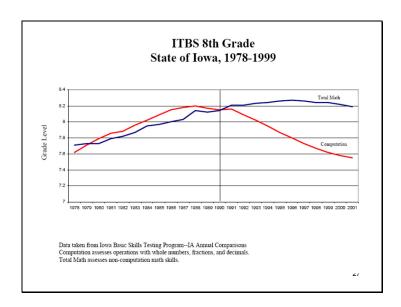
Since the units of J are $kg\cdot m^2\!/s^2,$ this expression becomes

$$\sqrt{1.86 \times 10^6 \frac{\text{kg} \cdot \text{m}^2}{\text{kg} \cdot \text{s}^2}} = 1.36 \times 10^3 \text{ m/s}$$

-- Zumdahl, 5th Ed. p. 218

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Chemistry?



There's more data, but it's all convergent. By all the measures we have, after 1990, across the nation, scores in the math we need in chemistry collapsed, but it went largely un-noted because it was hidden by "total math."

Vote for one:

Given the nature and magnitude of these data, how serious a problem is *computation* background for students needing to learn Gen Chem (in about 2003)?

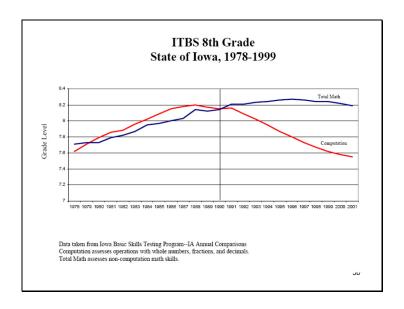
- A. Not very serious
- B. Serious
- C. Very Serious

2

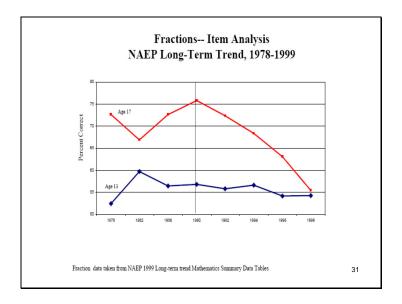
How serious is this? Let me let you decide. Please take a moment to read this slide, And then we'll vote.

All students			Grade 9		
	1998	1999	2000	2001	2002
Total Math	54	55	55	55	55
Problem Solving (Reasoning)	58	61	63	64	65
Procedures (Computation)	46	44	42	41	39

Virginia



Iowa



NAEP,

Vote for one:

Given the nature and magnitude of these data, how serious a problem is *computation* background for students needing to learn Gen Chem (in about 2003)?

- A. Not very serious
- B. Serious
- C. Very Serious

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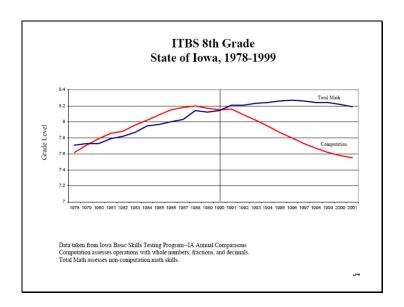
What's your view? How many vote for A? B? C? The average is: (was 95% C).

Has this been interesting data -- so far?

Why no state computation scores since 2002?

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Let's get up to date. You may have noticed that all of my state data stops in 2002. Why?



2001.

All students	Grade 9				
	1998	1999	2000	2001	2002
Total Math	54	55	55	55	55
Problem Solving (Reasoning)	58	61	63	64	65
Procedures (Computation)	46	44	42	41	39

2002. What happened in 2002? AP folks?

2002: NCLB

Mandates Tests on State Standards.

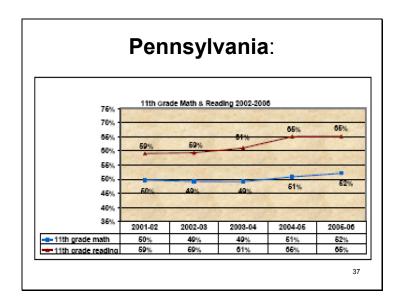
High test prep costs = most states stop *nationally normed* tests.

Since 2002: \$\$\$\$ reporting "total math"

But NO state reports computation.

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No Child Left Behind required each state to pay for a test customized to their own state standards. And, perhaps since adding a subtest is expensive, no state that I can find, and I've looked, has given a test that measured **computation** since 2002.



States do report "proficiency in total math" versus state standards. But that's the wrong variable. They want STEM majors, but they are not measuring preparation for STEM. And: how are these kids are doing versus the national average? Or versus China and India – the real economic competition?

For ~10⁺ year faculty:

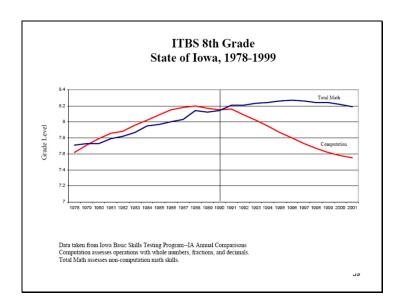
(Vote for ONE:)

Since 2002, I have seen the *computation skills* of first-year students:

- A. Improve substantially
- B. Improve
- C. Not change
- D. Decline
- E. Decline substantially

3

So we really don't know what's happened since 2002. But I can tell you that every group of chemistry instructors I have surveyed for the past 3 years, including you, has said that since 2002, the math problem in chemistry has gotten



Worse since 2001.



What went wrong in 1990? Dr Loveless says this:

"Nearly all state standards after 1990 were modeled on the 1989 NCTM Standards."

-- from Computation Skills, Calculators, and Achievement Gaps: An Analysis of NAEP Items

Tom Loveless, Brookings Institution, April 2004

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Take a look.

The Math Wars

Short history:

http://www.csun.edu/~vcmth00m/bshm.html

Long version:

http://www.csun.edu/~vcmth00m/AHistory.html

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What's this about? You can find more information in these references in my posted slides. But briefly:

The National Council of Teachers of Mathematics is a K-12 curriculum group.

Recommended for "INcreased attention"

In Grade 5-8 math:

- "Reasoning inductively and deductively"
- "Creating algorithms and procedures"

4

In the early 1990's, 48 of the 50 states adopted standards in math based on what are called the NCTM math standards. Those standards stated that if increased attention in math was given to reasoning,

Recommended for "decreased attention"

- "Memorizing rules and algorithms"
- "Finding exact forms of answers"
- "Manipulating symbols"
- "Relying on outside authority (teacher or answer key)"
- "Rote practice"
- "Paper and pencil fraction computation",

4

Attention to these topics could be decreased: Arithmetic, algebra, and fractions.

Recommended for "decreased attention"

- "Memorizing rules and algorithms"
- "Finding exact forms of answers"
- "Manipulating symbols"
- "Relying on outside authority (teacher or answer key)"
- "Rote practice"
- "Paper and pencil fraction computation",

45

The idea was well-intended: If you could reason, you would be spared the hard work Of learning math by memorizing and practice.

"By 2000, all but two states ... modeled their own curriculum standards on the NCTM's, and publishers revised math textbooks to conform with NCTM's prescriptions."

-- from

Computation Skills, Calculators, and Achievement Gaps:

An Analysis of NAEP Items

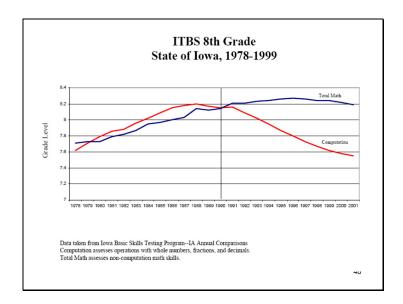
Tom Loveless, The Brookings Institution, April 2004

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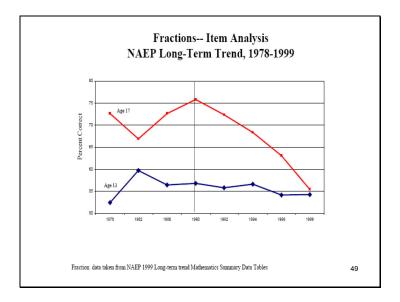
By 2000, every state except California and Massachusetts had adopted these standards, and nearly all K-12 textbooks changed of necessity to fit state standards.

All students	Grade 9				
	1998	1999	2000	2001	2002
Total Math	54	55	55	55	55
Problem Solving (Reasoning)	58	61	63	64	65
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So, teachers taught and students learned math reasoning. See those scores?



But the theory about reasoning didn't work, and scores in computation collapsed.



Why Didn't Reasoning Help With Calculations?

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You might be asking

2010-2012: New Cognitive Science Consensus

2012 Jargon-Free Summary: (6 pages)Putting Students on the Path to Learning by Clark, Sweller, and Kirschner at:

http://www.aft.org/pdfs/americaneducator/spring2012/Clark.pdf

(search "Clark American Educator 2012")

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Just in the past 3 years, researchers in cognitive science have finally agreed on the answer to the question at the heart of our role as chemistry educators, which is: What do we tell students that **they** need to **do** in order to become **proficient** in **solving** science problems?

There is a new article out that explains this research consensus in six easy-to-read pages.

This is your homework. But let me try to summarize. Here's what those who study how the brain works say that we need to tell our students:

2012: Cognitive Science Says:

- Long Term Memory (LTM) is where you store information. Human LTM is enormous.
- Working Memory (WM), where you solve problems, is limited.

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Please read this And this

2012: Cognitive Science Says:

- In working memory, you can manipulate up to 4 chunks of info you have not memorized plus all you have memorized in Long Term Memory.
- So, **memorization** of fundamentals is crucial for solving problems.
- Each individual must also construct mental models of concepts to tag new info with meaning in your LTM.

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Here is what it means. To solve problems in a field: you first need to **memorize** the core knowledge of the discipline, while at the same time you construct a conceptual framework to tag this new information with meaning.

I know that for some of us, this finding on the m-word is disappointing. In the Monty Python Group, we don't like it either. But in 2012 this is now tested, proven science, and in science we pledge to follow this rule:

"If nature does not answer first what we want, it is better to take what answer we get."

-- J. Willard Gibbs, Lecture XXX (courtesy of Bob Hanson)

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We need to accept the science.

Recommended for "decreased attention"

- "Memorizing rules and algorithms"
- "Finding exact forms of answers"
- "Manipulating symbols"
- "Relying on outside authority (teacher or answer key)"
- "Rote practice"
- "Paper and pencil fraction computation",

55

The new cognitive science explains why "decreasing memorizing and practice" did not work as a learning strategy (but to be fair, in 1989, working memory was not well understood.)

2012: Cognitive Science Says:

- In working memory, you can manipulate up to 4 chunks of info you have not memorized plus all you have memorized in Long Term Memory.
- So, **memorization** of fundamentals is crucial for solving problems.
- Each individual must also construct mental models of concepts to tag new info with meaning in your LTM.

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Way more important, thanks to science, we can now give our students clear and effective advice on how to learn math and science. And this advice is consistent with how all of us learned chemistry.

Conditions:

This research consensus applies:

- Only for Math and Science (WSDs)
- Only Undergraduates and below

5

There are exceptions to the rules. Be sure to read the article.

Impact of Cognitive Science

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The new cognitive science has already had impact.

Since 2010: 45 States Adopt K-12 Common Core Standards

Good on Math!

- "Fluently add and subtract within 20." (Grade 2)
- "Fluently ... multiply whole numbers using the standard algorithm...." (Grade 5)
- Fluently means: fast from memory.

5

Since 2010, 45 states have adopted the new common core math standards. And they are pretty good. See the word "fluency"? That's the "fast recall" from cognitive science, and it means a restored emphasis on mental arithmetic in K-12. But...

New Standards Impact: In 10-20 years

60

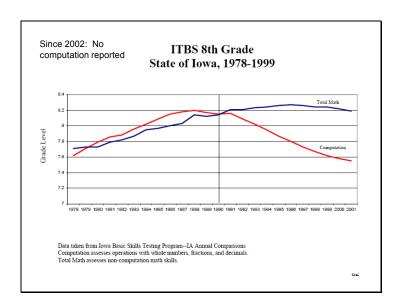
You are not going to see the impact of these standards in your entering students for at least 10-20 years.

Why?

- Years to create books and tests (2015)
- K-12 book adoption over 6-10 years
- Students + teachers in abrupt transition
- Moving kids from grades 2 to 12 under standards that work = 10 years.
- Ideological, emotional resistance to drill

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Here's why change in K-12 is going to take a long time. Take a look.



Scores fell in Iowa for at least 12 years. Change in K-12 does not happen quickly.

Summary: In 2012

63

Let's see where we are.

For the next 10-15 years, will most students entering college be able to do chem math?

64

Please take a look at this question, and now let's vote. How many vote yes, raise your hand? How many no?

Is it their fault?

65

How many vote yes? No?

Wonderful news. Now we know what works.

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But, thanks to cognitive science, now we have much better understanding of how we can teach needed math in a hurry.

The Monty Python Experiment:

In lecture: Time for activities that construct conceptual understanding.

In homework:

- *Teach* exponentials, fractions, algebra, logarithms.
- Then apply to chem.

6

In our Monty Python lessons, so that instructors have more time in lecture for concepts, in homework we harness cognitive science to teach these four math skills.

Resources on the New Cognitive Science

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Here are some additional readings on the new cognitive science.

Short Introductory Articles

1. Spring 2012: 6-pages on cognition and problem solving:

Putting Students on the Path to Learning by Clark, Sweller, and Kirschner at:

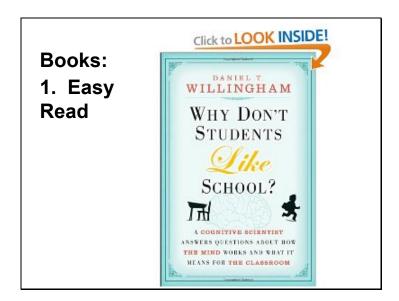
http://www.aft.org/pdfs/americaneducator/spring2012/Clark.pdf

(search "Clark American Educator 2012")

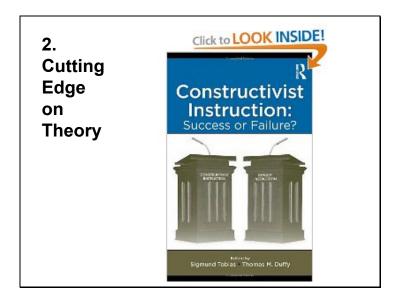
2. Short, jargon-free articles by cognitive scientist Daniel Willingham on topics including critical thinking:

http://www.danielwillingham.com/articles.html

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Plus two books: Easy



and challenging.

These slides are posted at www.ChemReview.Net at the **BCCE** tab.

Feel free to use these data.

Done! Opposing Views?

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The slides are posted here. Thank you for your patience!